

# FMI036 Superconductivity and Low Temperature Physics

## Out line lecture 1

### History

Kamerling-Onnes

Liquefaction of Helium 1908

Resistivity of Mercury dropped to zero (1911)

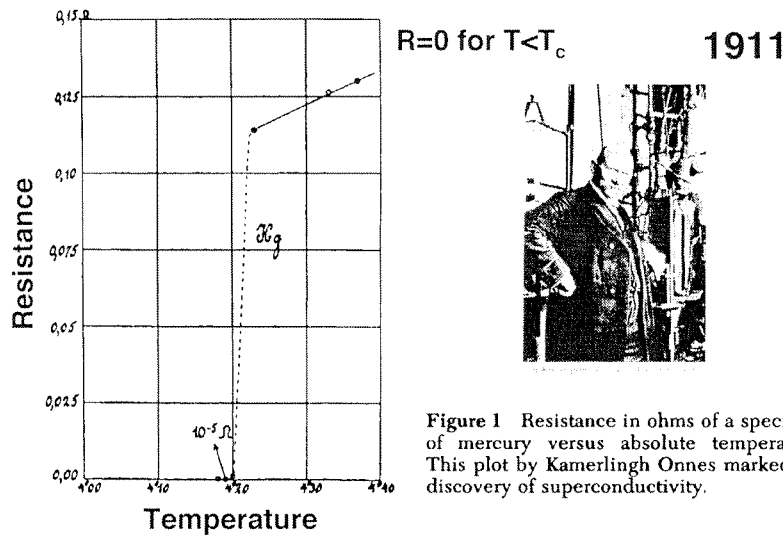


Figure 1 Resistance in ohms of a specimen of mercury versus absolute temperature. This plot by Kamerlingh Onnes marked the discovery of superconductivity.

Mercury  $T_c=4.15$  K, impurities did not affect  $T_c$ .

Many more elements were found to be SC shortly after the init

### Electro magnetic properties of Superconductors (SC)

$R=0$ , Critical temperature  $T_c$

$B=0$ , Meissner effect, screening currents c.f. perfect conductor. Penetration depth  $\lambda$

Maximum Magnetic field: The critical field  $H_c$  and its temperature dependence.  $T, H, I$  surface.

### Thermal Properties:

Specific heat  $C_p$  has a discontinuity at  $T_c$ ,  $T^3$ , jump indicates phase transition

Heat conductivity graph, perfect electrical conductor very poor thermal conductor.

The electronic part of  $\kappa$  decreases rapidly below  $T_c$ , this indicates an energy gap for excitations,  $\Delta=1.76 k_B T_c$ .

### Overview of Periodic table

Which elements are SC: Nb, Ta, Pb, Sn, In, Al, ... Nb highest  $T_c=9.2$ K.

Two regions in the periodic table

Which elements are not SC: coin metals, magnetic metals

Which elements are not superconducting, Alkali, rare earth, magnetic, and coin metals.

Why are good conductors such as Cu, Ag, not SC, whereas more resistive metals such as Pb and Sn are? This indicates that the mechanism has something to do with electron phonon scattering.

**KNOWN SUPERCONDUCTIVE ELEMENTS**

\* BLUE = AT AMBIENT PRESSURE  
\* GREEN = ONLY UNDER HIGH PRESSURE

1	IA																					0				
1	H																	2	He							
2	Li	Be																	5	B	C	N	O	F	10	Ne
3	Na	Mg				III B	IV B	V B	VI B	VII B	VIII B		IX B		X B	13	Al	Si	P	S	Cl	18	Ar			
4	K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	31	Ga	Ge	As	Se	Br	36	Kr						
5	Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	49	In	Sn	Sb	Te	I	54	Xe						
6	Cs	Ba	*La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	81	Tl	Pb	Bi	Po	At	86	Rn						
7	Fr	Ra	+Ac	Rf	Ha	106	107	108	109	110	111	112	SUPERCONDUCTORS.ORG													

* Lanthanide Series	58	59	60	61	62	63	64	65	66	67	68	69	70	71
	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu
+ Actinide Series	90	91	92	93	94	95	96	97	98	99	100	101	102	103
	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr

### Comparing properties of different elements

Table with different parameters  $T_c$ ,  $H_c$ , ...  
Explaining other parameters:  $\xi$ ,  $\lambda$ ,  $\kappa$ ,  $\Delta$ , ..

Parameters for superconducting elements

	$T_c$	Density	$\lambda$	$\xi$	$\kappa$	$2\Delta$	$H_c$	$\Theta$ Debye	$\gamma$
	K	kg/l	nm	nm		meV	Gauss	K	mJ/mol/K
Nb	9.250	8.57	39	38	1.03	3.050	2060.0	276	7.80
Pb	7.196	11.34	37	83	0.45	2.730	803.0	96	3.10
V	5.400	6.11				1.600	1408.0	383	9.82
Ta	4.470	16.65				1.400	829.0	258	6.15
Sn	3.722	7.31	36	230	0.16	1.150	305.0	195	1.78
In	3.408	7.31	21	440	0.05	1.050	281.5	109	1.67
Re	1.697	21.01				0.514	198.0	430	2.35
Al	1.175	2.70	16	1600	0.01	0.340	104.9	420	1.35
Ga	1.083	5.91				0.328	58.3	325	0.60
Mo	0.915	9.01				0.277	96.0	460	1.83
Zn	0.850	7.13				0.257	54.0	310	0.66
Zr	0.610	6.51				0.185	47.0	290	2.77
Cd	0.517	8.65	110	760	0.15	0.157	28.0	209	0.69
Ti	0.400	4.57				0.121	56.0	415	3.30
Hf	0.126	13.31				0.038	12.7	254	2.21
W	0.015	19.30				0.005	1.2	383	0.90

## Other Superconducting , compounds and alloys

Alloys behave differently from elements (Type II) allows high field e.g. NbTi

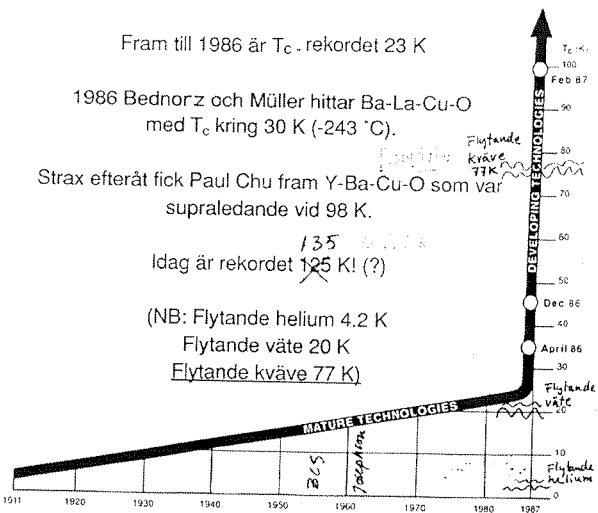
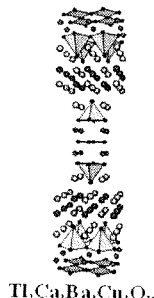
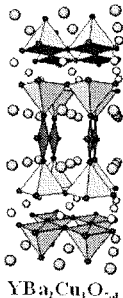
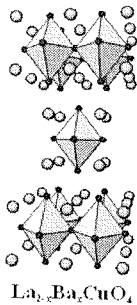
A15 Compounds NbSn<sub>3</sub>, T<sub>c</sub>≈23K

Heavy Fermions, UBe13, UPt3 magnetic interaction f electrons => renormalized e-mass.

Organic superconductors, fullerenes, nanotubes

There was a rapid increase of the best T<sub>c</sub>'s with the discovery of the High T<sub>c</sub> Superconductors (HTS)  
Anisotropic structure and anisotropic gap.

1986: Bednorz and Müller,	LaBaCuO	36K
1987: Paul Chu,	YBa <sub>2</sub> Cu <sub>3</sub> O <sub>7</sub>	93K
1988:	Bi <sub>2</sub> Sr <sub>2</sub> Ca <sub>2</sub> Cu <sub>3</sub> O <sub>x</sub>	110K
2001:	MgB <sub>2</sub>	39K



## Overview of different theories

1934 **The two fluid model**, Gorter and Casimir (phenomenological)

One fluid with "super electrons" and one fluid with "normal electrons", n<sub>s</sub>, n<sub>n</sub>

1935 **London equations**, Fritz and Heinz London (phenomenological)

Describes electromagnetics of the superconductor, based on the two fluid model

1951 **Ginzburg Landau Theory**, Starts from phase transitions, valid near T<sub>c</sub>, explains vortecies

GL describes phase transitions, Strictly speaking only valid close to T<sub>c</sub> but it work pretty well also at lower temperature. The theory explains vortices and other phenomena when the order parameter changes over short distances.

1959 **BCS theory**, "Full" microscopic theory (does not explain HTS)

Describes a quantum mechanical ground state for the superconducting condensate. Many properties can be calculated.



John Bardeen, Leon Cooper and J. Robert Schrieffer



Vitaly Ginzburg

2007 There is still no accepted theory for High T<sub>c</sub> superconductors.

## Overview of Superconducting devices

Power applications

Strong magnets

Electronic devices based on tunnel junctions

SQUIDs Magnetometers

SIS mixers, microwave detectors

RSFQ logic

High Q rf- and microwave- filters

### The two fluid model

It seems as if there was two different fluids mixed, one with "superconducting electrons" and one with "normal electrons". On this point there is a clear relation to superfluid helium.

The super fluid would carry current without resistance and without entropy whereas the normal fluid would carrying entropy and be subject to scattering.

Temperature dependence of the densities,  $n_s$  and  $n_n$

Examples: Conductivity, Thermal conductivity, Thermo electric effects.

Absence of electric field also leads to absence of thermoelectric effects.

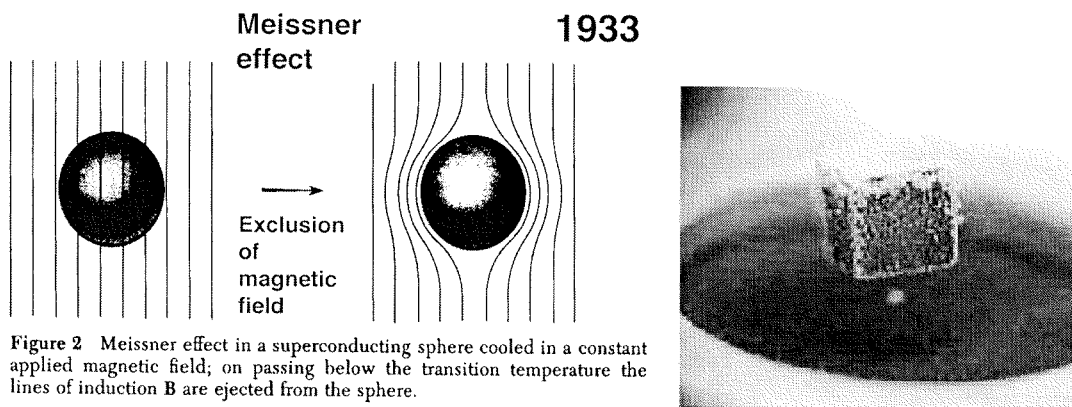
### Meissner effect

$R=0$  implies that the electric field in a superconductor is zero also.

Applying Faradays law to a ring of superconductor implies that the Magnetic flux is constant in a superconducting ring.

$\oint E \cdot dl = -\frac{\partial \Phi}{\partial t} = -A \frac{\partial B}{\partial t}$  implies  $\partial B / \partial t = 0$ . In fact, not only  $\partial B / \partial t = 0$  but also  $B=0$ .

Perfect dia-magnetism,  $B = \mu_0(H+M) = \mu_0(1+\chi)H$ , Superconductor:  $\chi = -1$



### Type I versus Type II superconductors.

Type I: Either Superconducting or Normal

$B=0$  up to  $H_c$ , graph  $M$  versus  $H$ .

Positive SN interface energy  $\Rightarrow$  minimize number of interfaces

Intermediate state, few domains

Type II:

$B=0$  up to  $H_{c1}$  and gradually increasing up to  $H_{c2}$

Graph  $M$  versus  $H$

Negative SN interface energy.

Mixed state between  $H_{c1}$  and  $H_{c2}$ , many domains