

Örning 8 - Lösningar

①

32.2

Vi behandlar telefonkabel som en spole:

Då gäller:

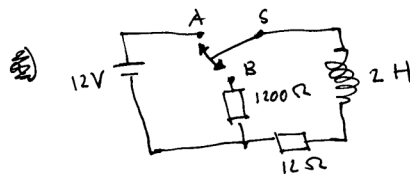
$$L = \frac{\mu_0 N^2 A}{\ell} = \frac{4\pi \cdot 10^{-7} \cdot 70^2 \cdot \pi \cdot (6.5 \cdot 10^{-3})^2}{0.6} = 1.36 \mu H$$

32.15

$$a) L = \frac{\mu_0 N^2 A}{\ell} = \frac{\mu_0 (120)^2 \cdot \pi \cdot (5 \cdot 10^{-3})^2}{0.09} = 15.8 \mu H$$

$$b) \phi_B' = \frac{\mu_m}{\mu_0} \phi_B \Rightarrow L = \frac{\mu_m N^2 A}{\ell} = 800 \cdot 15.8 \cdot 10^{-6} = 12.6 \mu H$$

32.26



$$a) I = \frac{E}{R} = \frac{12V}{12\Omega} = 1A$$

$$b) I_{initial} = 1A : \quad \begin{aligned} \Delta V_{12} &= 1A \cdot 12\Omega = 12V \\ \Delta V_{1200} &= 1A \cdot 1200\Omega = 1200V \\ \Delta V_L &= \Delta V_{12} + \Delta V_{1200} = 1212V \end{aligned}$$

$$c) I(t) = I_{max} e^{-Rt/L}$$

$$\frac{dI}{dt} = -I_{max} \cdot \frac{R}{L} e^{-Rt/L} \quad \text{och} \quad -L \frac{dI}{dt} = \Delta V_L = I_{max} R e^{-Rt/L}$$

Vi löser då ekvationen

$$12V = (1212V) \cdot e^{-1212t/2} \Rightarrow t = 7.62 \mu s$$

32.40

$$\mathcal{E}_2 = -M \frac{dI_1}{dt} = - (1 \cdot 10^{-4} H) (1 \cdot 10^4 A/s) \cdot \cos 1000t$$

$$(\mathcal{E}_2)_{max} = 1V$$

32.59

$$a) Q = Q_{max} e^{-\frac{Rt}{2L}} \cos \omega_d t \Rightarrow I_{max} \propto e^{-\frac{Rt}{2L}}$$

$$0.500 = e^{-\frac{Rt}{2L}} \Rightarrow \frac{Rt}{2L} = -\ln 0.5 \Rightarrow t = -\frac{2L}{R} \ln(0.5) = -0.693 \cdot \frac{2L}{R}$$

$$b) \quad U_0 \propto Q_{\max}^2 \quad \text{och} \quad U = 0.5 U_0 \quad (2)$$

$$\text{då får vi } Q = \sqrt{0.5} Q_{\max} = 0.707 Q_{\max}$$

$$t = -\frac{2L}{R} \ln(0.707) = \underline{\underline{0.347 \cdot \frac{2L}{R}}}$$
